

EE 230

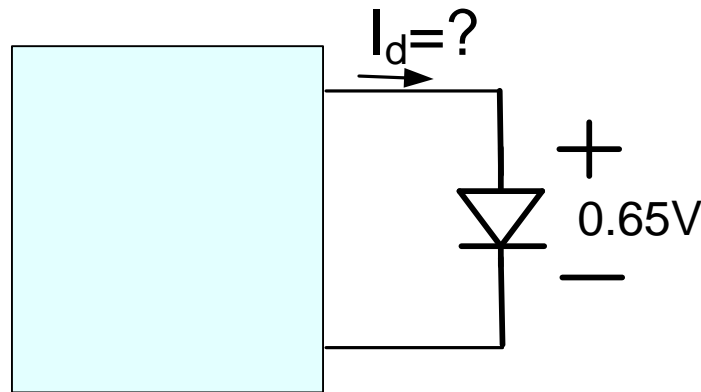
Lecture 28

Nonlinear Circuits using Diodes

- Rectifiers
- Precision Rectifiers
- Nonlinear function generators

Quiz 18

If a diode has a value of $I_s=1\text{E-}14\text{A}$ and the diode voltage is $.65\text{V}$, what will be the diode current if operating at $T=300\text{K}$?



And the number is ?

1

3

8

5

4

2

6

9

7

And the number is ?

1

3

8

5

4

2

3

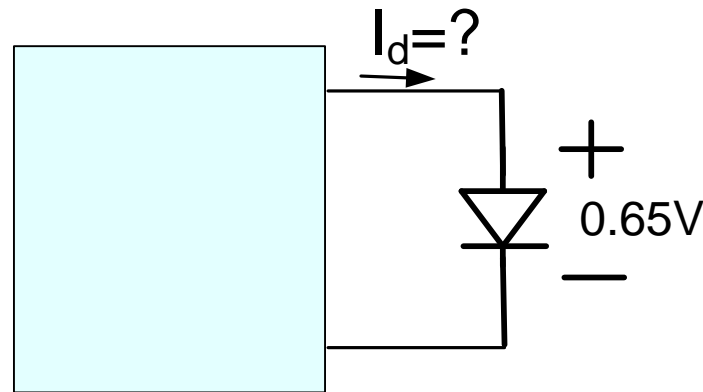
6

9

7

Quiz 18

If a diode has a value of $I_S=1E-14A$ and the diode voltage is .65V, what will be the diode current if operating at $T=300K$?



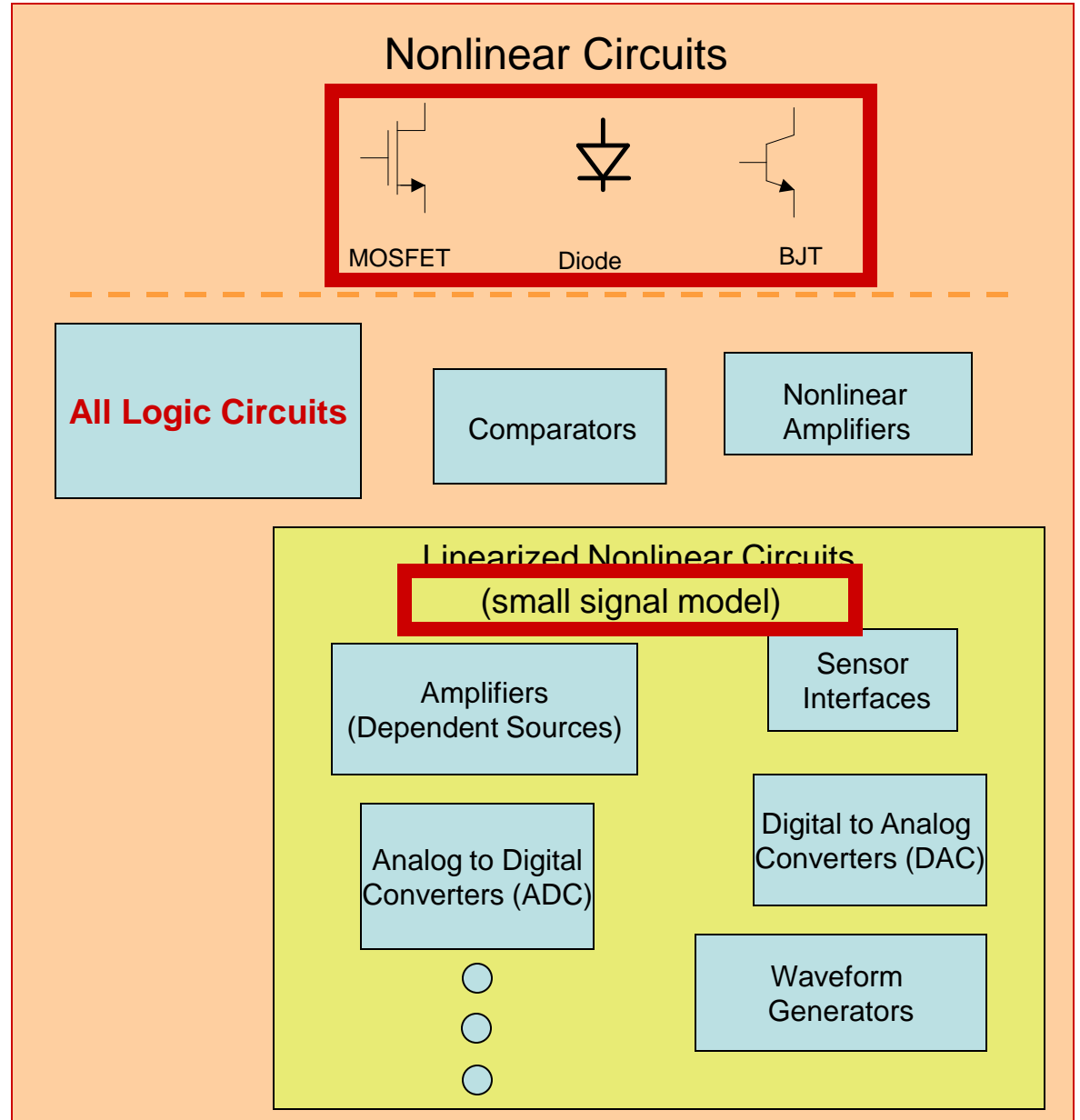
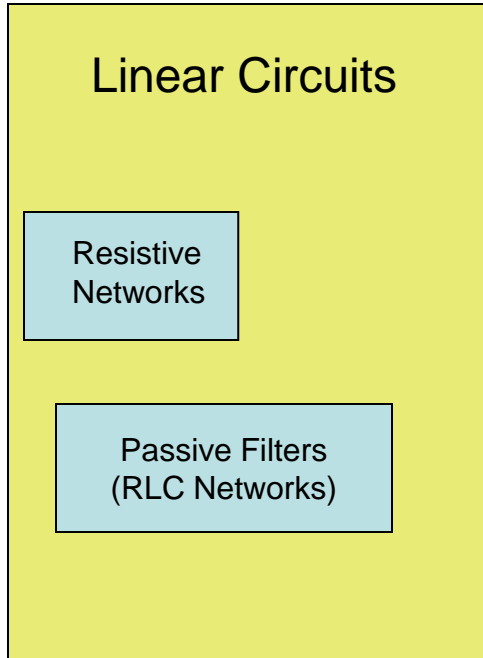
Solution:

$$I_d = I_S \left(e^{\frac{V_d}{V_t}} - 1 \right)$$

$$I_d = 1E-14 \left(e^{\frac{0.65}{300 \cdot 8.63E-5}} - 1 \right) = 1E-14 \cdot 8E10 = 800\mu A$$

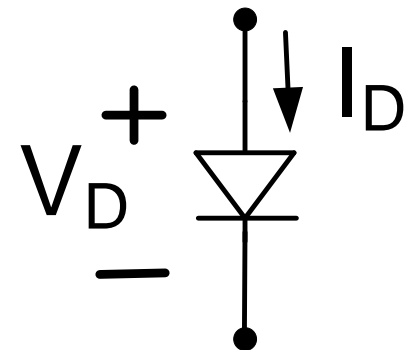
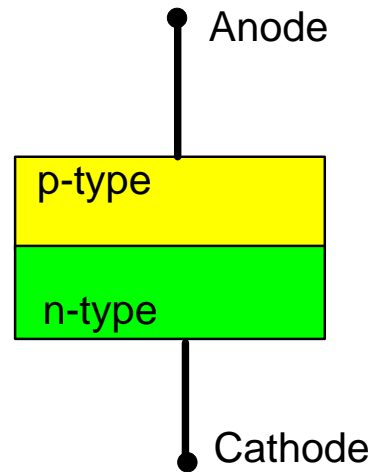
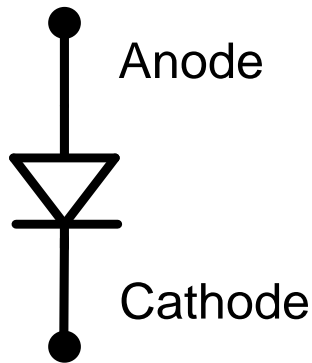
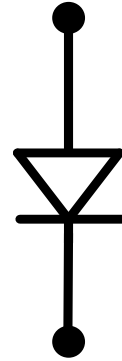
Review from Last Time:

The Real Electronics World



Review from Last Time:

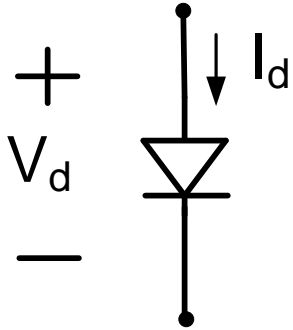
The Diode



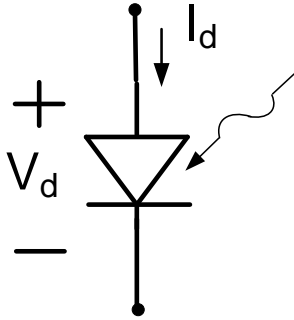
Review from Last Time:

Types of Diodes

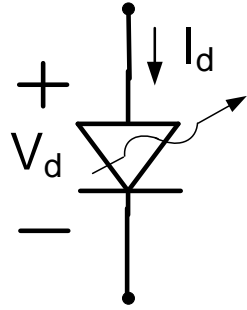
pn junction diodes



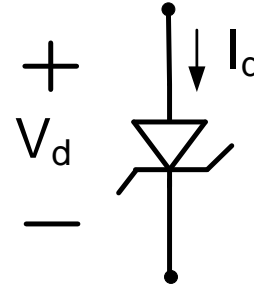
Signal or Rectifier



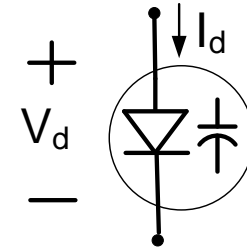
Pin or Photo



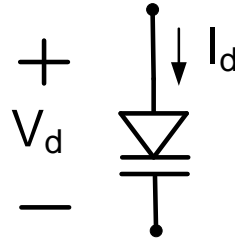
Light Emitting LED
Laser Diode



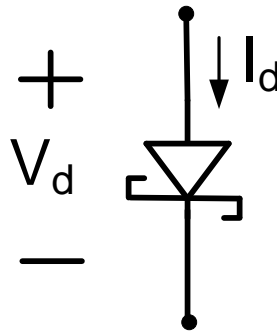
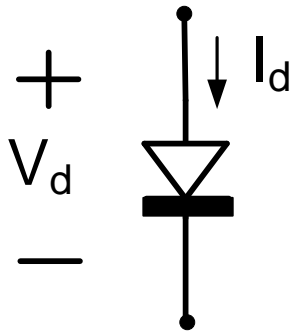
Zener



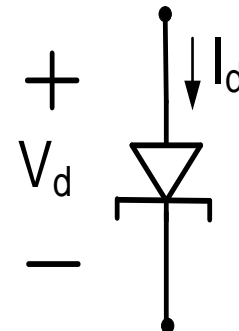
Varactor or Varicap



Metal-semiconductor junction diodes

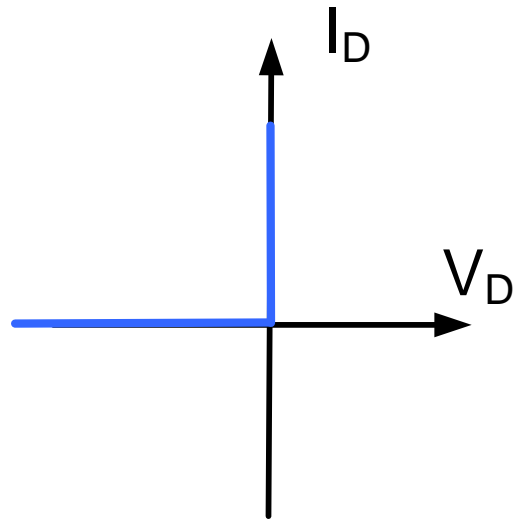


Schottky Barrier



Review from Last Time:

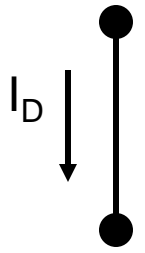
The Ideal Diode



$$I_D = 0 \quad \text{if} \quad V_D \leq 0 \quad \text{“OFF”}$$
$$V_D = 0 \quad \text{if} \quad I_D > 0 \quad \text{“ON”}$$

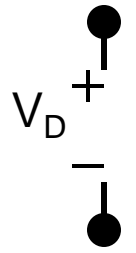


“ON”



$$I_D > 0$$

“OFF”



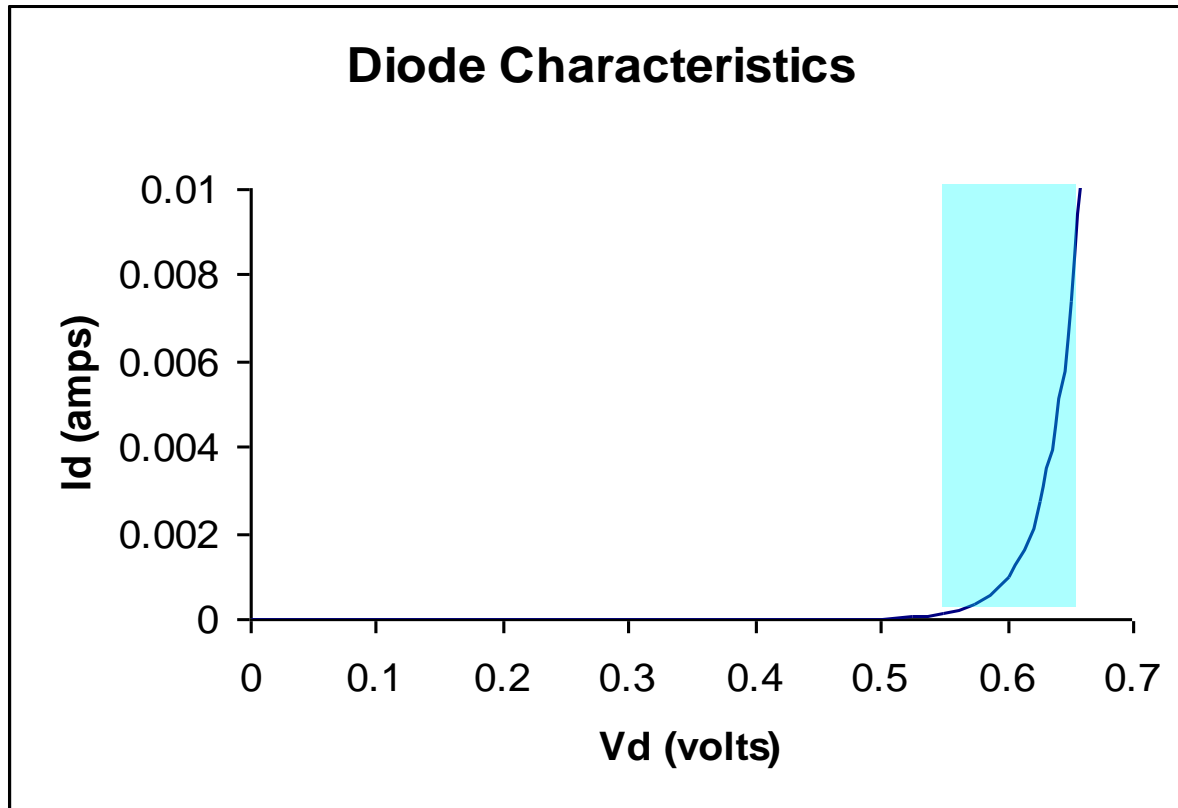
$$V_D \leq 0$$

Valid for

Review from Last Time:

Diode equation (silicon pn junction diodes)

$$I_d = I_s \left(e^{\frac{V_d}{V_t}} - 1 \right)$$

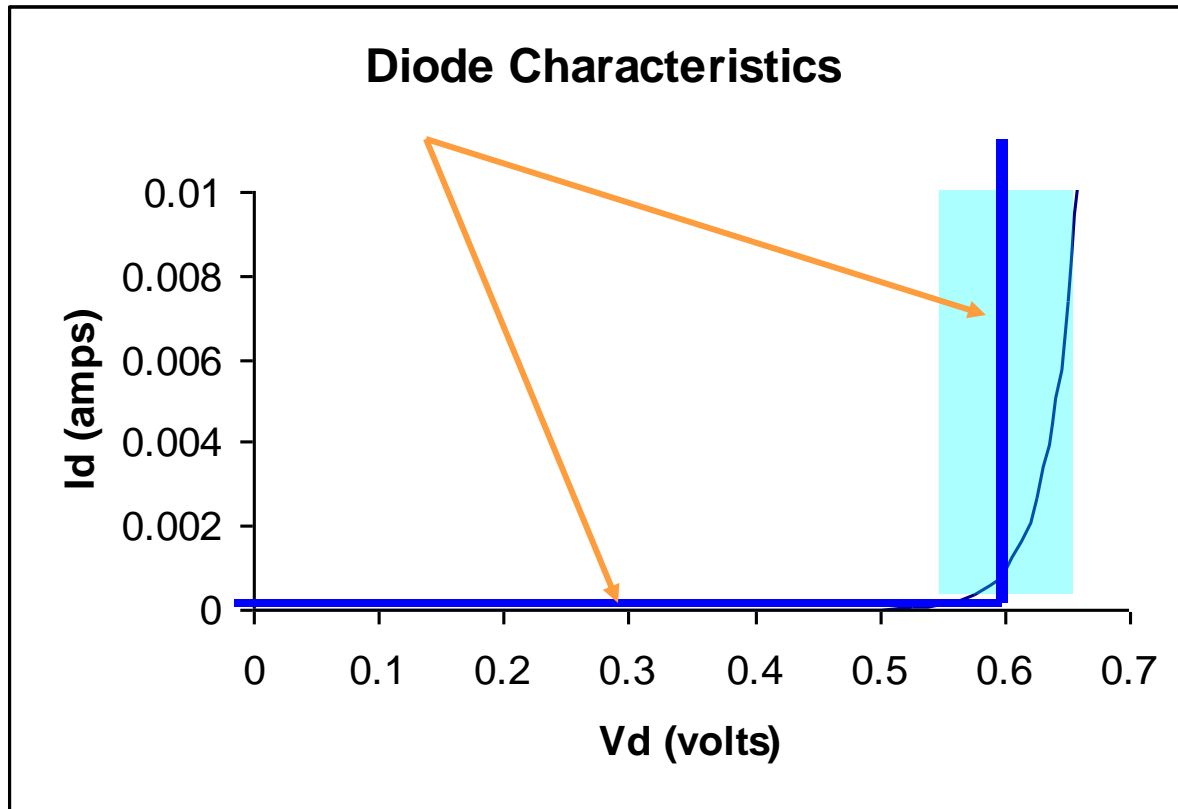


Widely Used Piecewise Linear Model

Review from Last Time:

A more accurate approximation to the diode equation

$$I_d = I_S \left(e^{\frac{V_d}{V_t}} - 1 \right)$$



More accurate pn junction
diode model:



$$\begin{array}{ll} I_d = 0 & V_d < 0.6V \\ V_d = 0.6V & I_d > 0 \end{array}$$

Review from Last Time:

A more accurate approximation to the diode equation

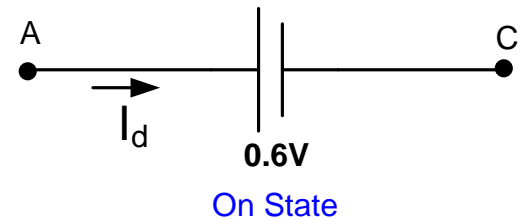
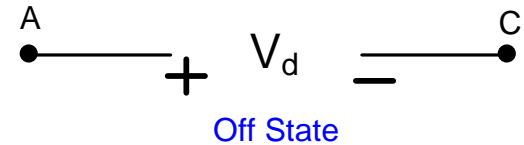
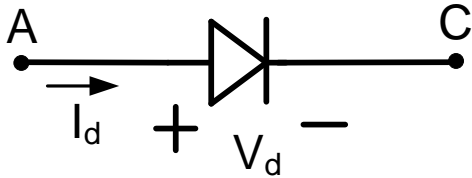
$$I_d = I_S \left(e^{\frac{V_d}{V_t}} - 1 \right)$$

Piecewise Linear Model

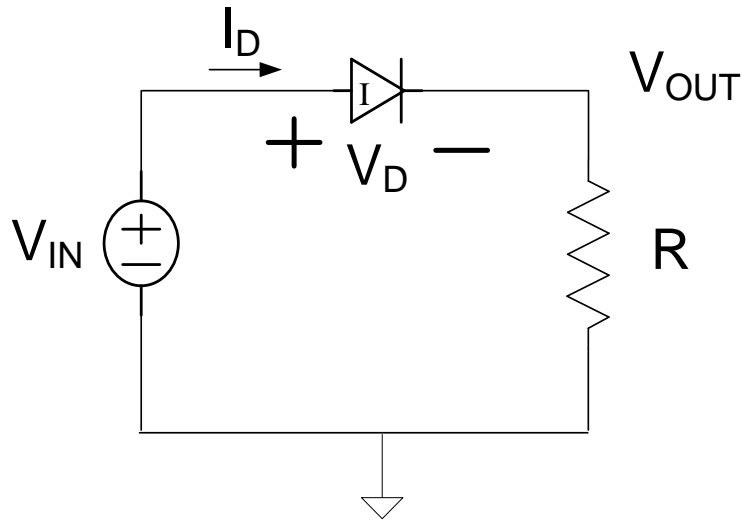
$$I_d = 0 \quad V_d < 0.6V$$

$$V_d = 0.6V \quad I_d > 0$$

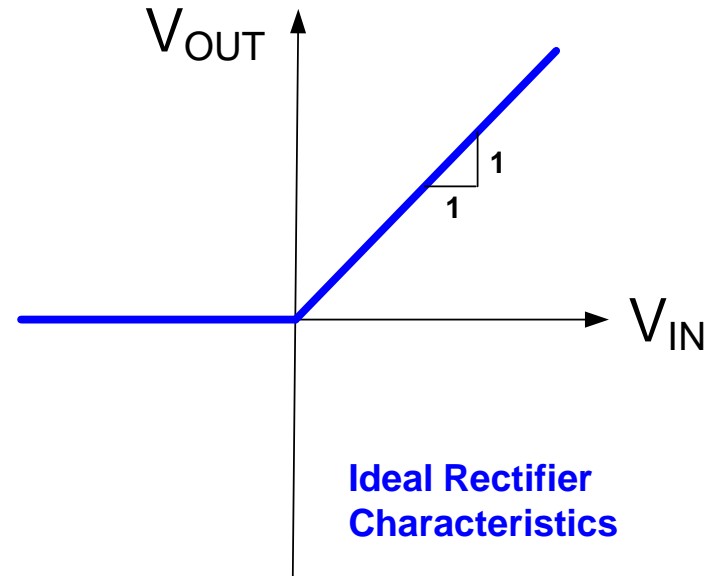
Equivalent Circuit



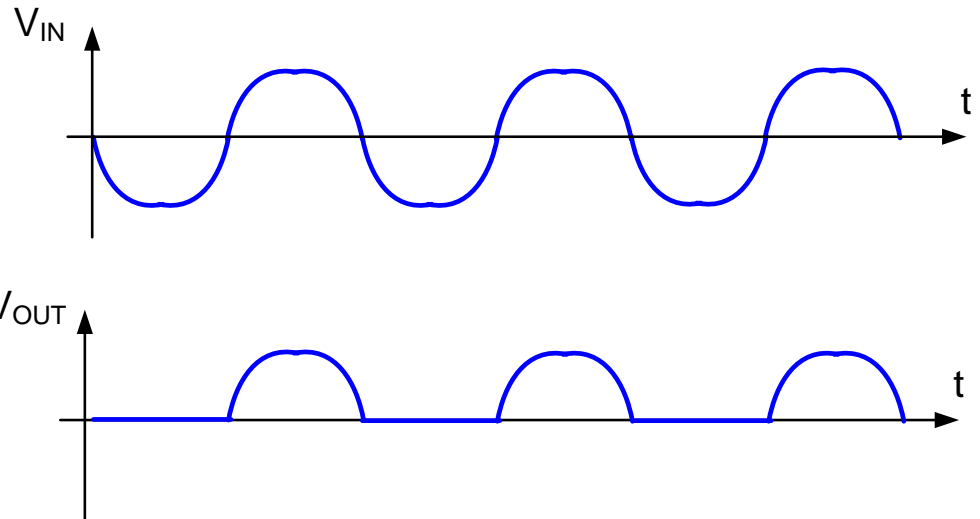
Review from Last Time:



Diode rectifier circuit

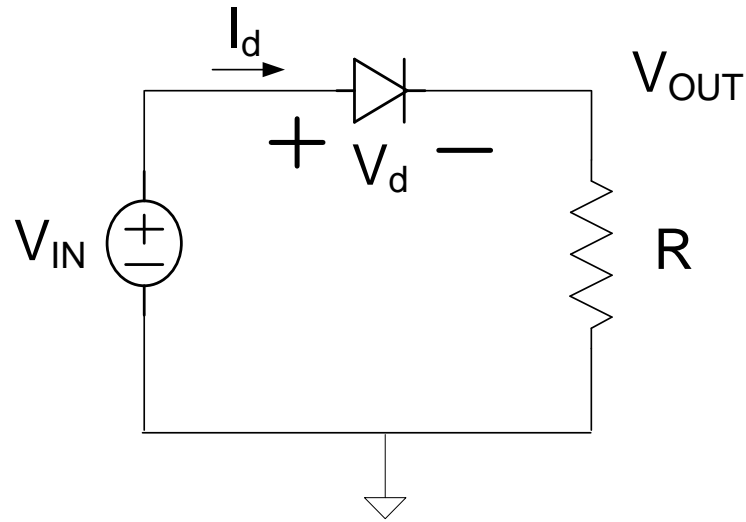


If $V_{IN} = V_M \sin \omega t$



Serves as a rectifier – very useful function !

Consider again the basic rectifier circuit



Analyze with piecewise linear model $I_d = 0$ $V_d \leq 0.6V$

$V_d = 0.6V$ $I_d > 0$

Case 1 $I_d = 0$

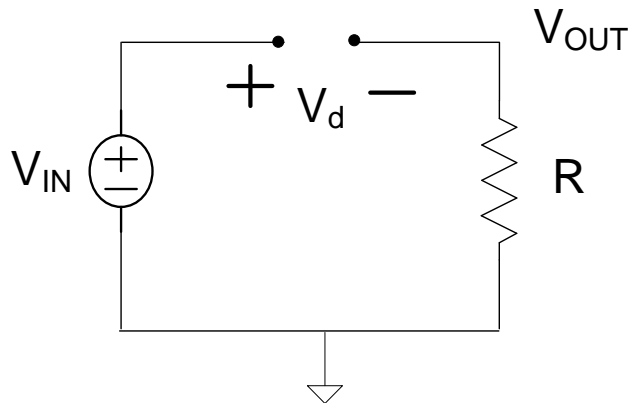
$$V_{OUT} = 0$$

valid for $V_d \leq 0.6V$

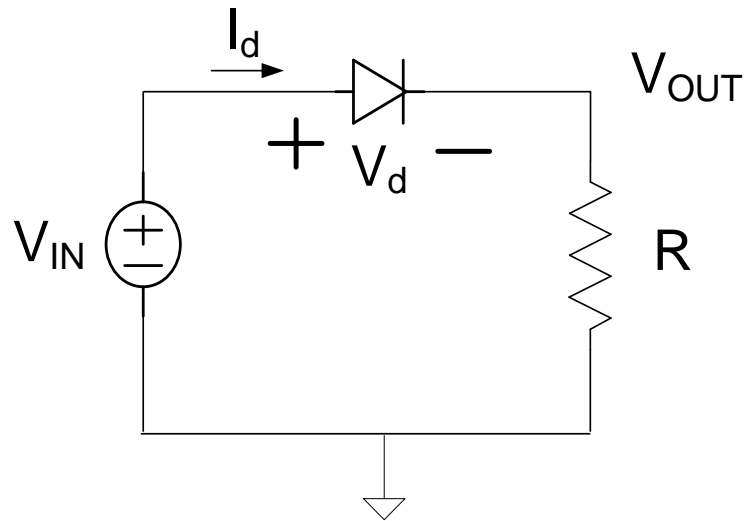
but $V_d = V_{IN}$

\therefore valid for

$$V_{IN} \leq 0.6V$$



Consider again the basic rectifier circuit



Analyze with piecewise linear model

$$I_d = 0 \quad V_d < 0.6V$$

$$V_d = 0.6V \quad I_d > 0$$

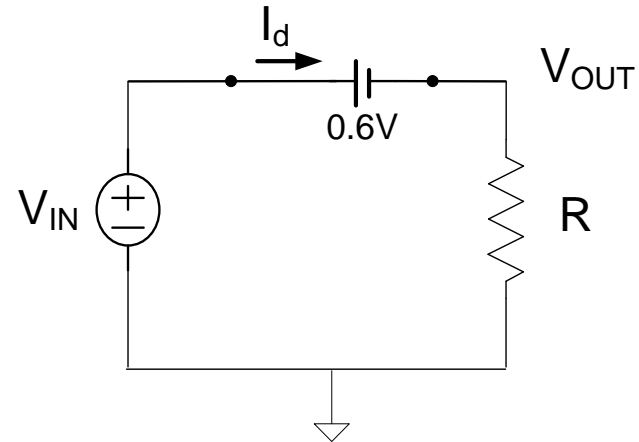
Case 2 $V_d = 0.6V$

$$V_{OUT} = V_{IN} - 0.6V$$

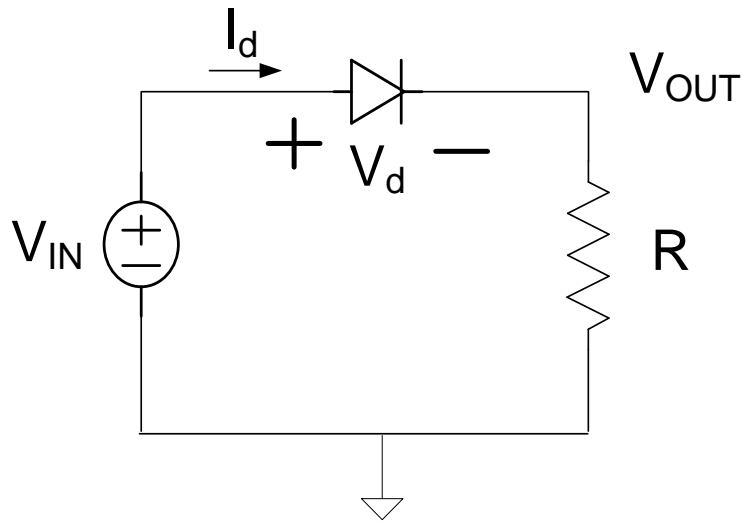
valid for $I_d > 0$

but $I_d = \frac{V_{IN} - 0.6V}{R}$

\therefore valid for $V_{IN} > 0.6V$



Consider again the basic rectifier circuit

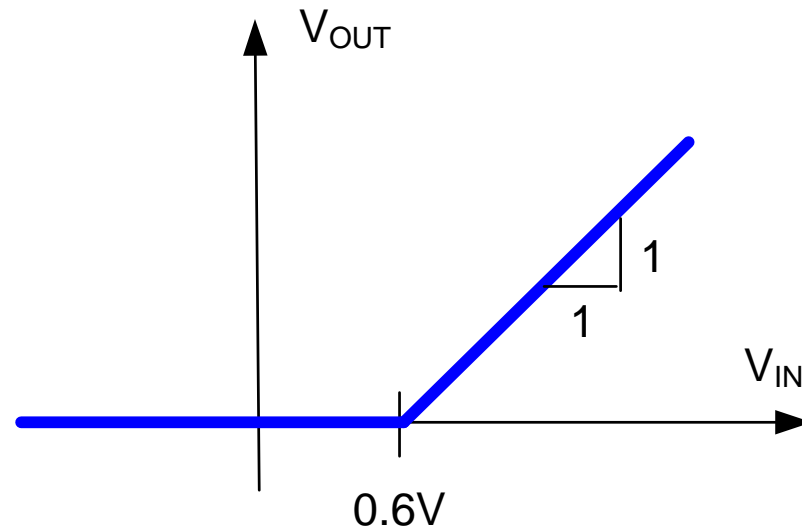


Analyze with piecewise linear model

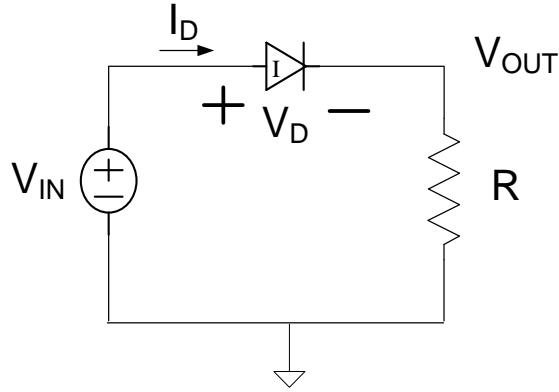
$$\begin{aligned} I_d &= 0 & V_d < 0.6V \\ V_d &= 0.6V & I_d > 0 \end{aligned}$$

Solution summary:

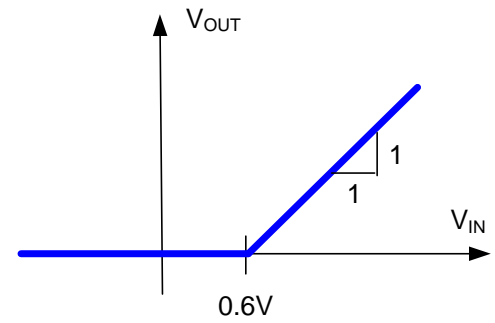
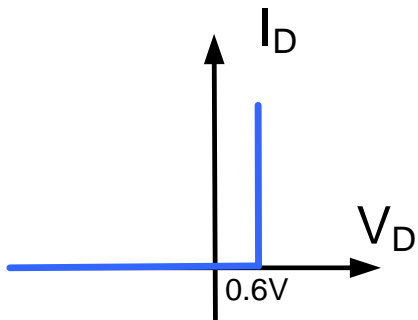
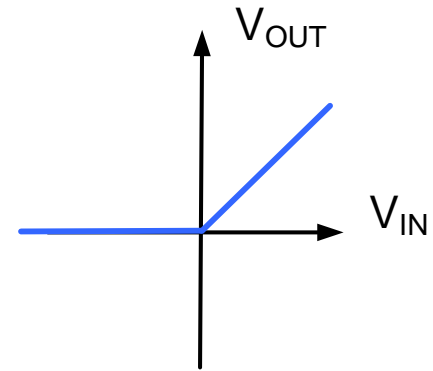
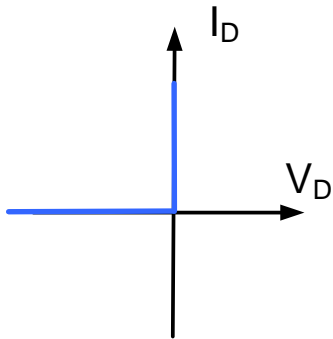
$$V_{OUT} = \begin{cases} 0 & V_{IN} \leq 0.6V \\ V_{IN} - 0.6V & V_{IN} > 0.6V \end{cases}$$



Performance Limitations of Diode Rectifier Circuit

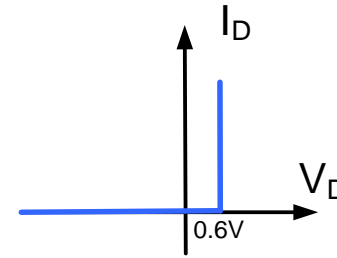
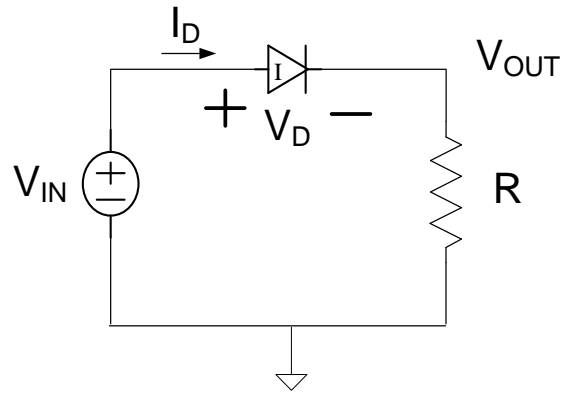


Diode rectifier circuit

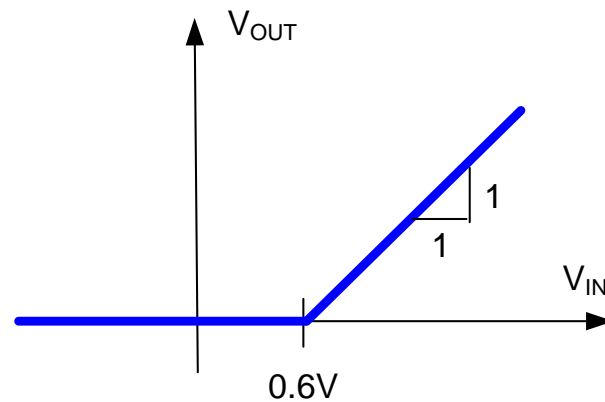


shift in break point

Performance Limitations of Diode Rectifier Circuit

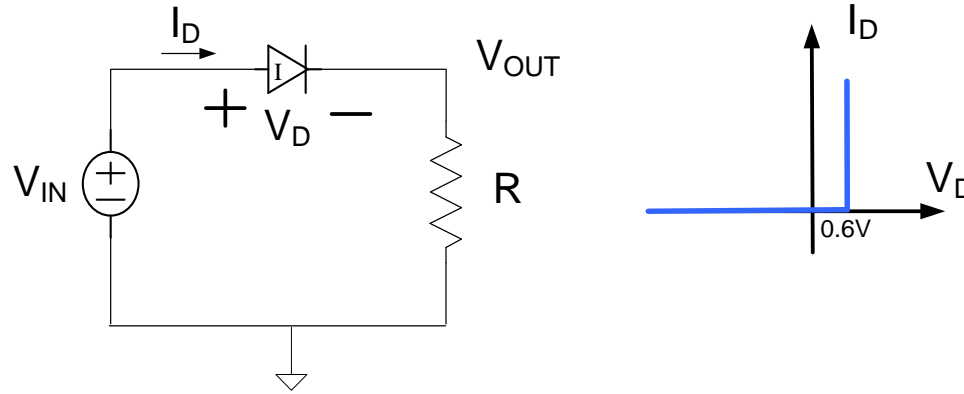


Diode rectifier circuit



$$V_{OUT} = \begin{cases} 0 & V_{IN} \leq 0.6V \\ V_{IN} - 0.6V & V_{IN} > 0.6V \end{cases}$$

Performance Limitations of Diode Rectifier Circuit

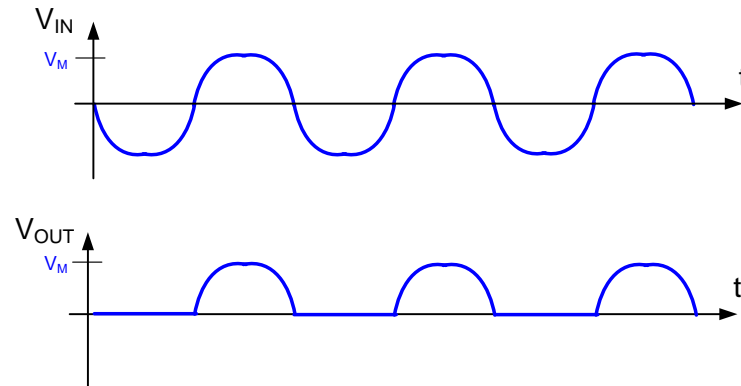


Diode rectifier circuit

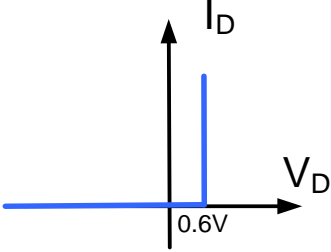
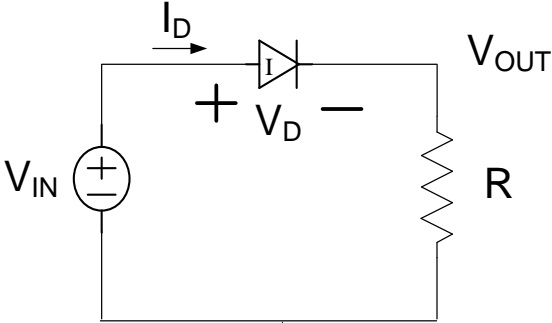
$$V_{OUT} = \begin{cases} 0 & V_{IN} \leq 0.6V \\ V_{IN} - 0.6V & V_{IN} > 0.6V \end{cases}$$

Consider $V_{IN} = V_M \sin \omega t$ for $V_M = 50V$, $V_M = 1V$ and $V_M = 0.5V$

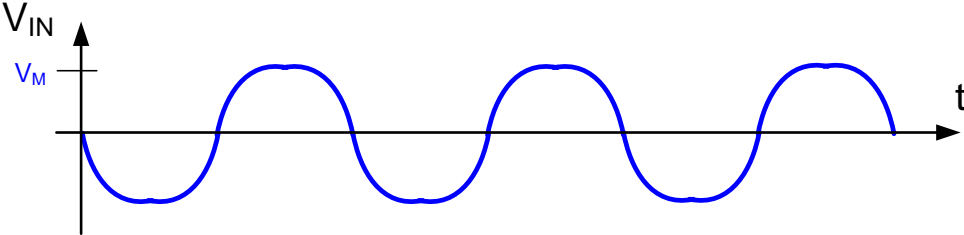
Desired output:



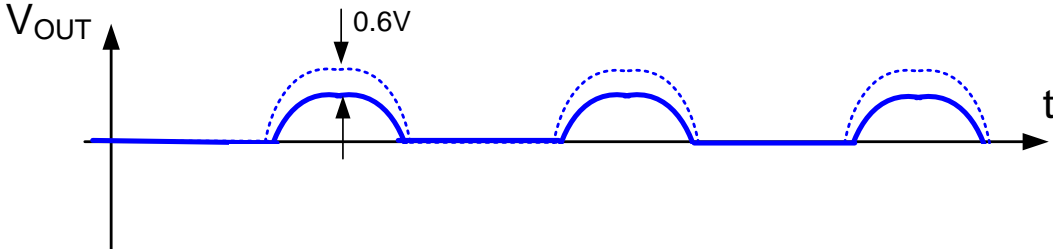
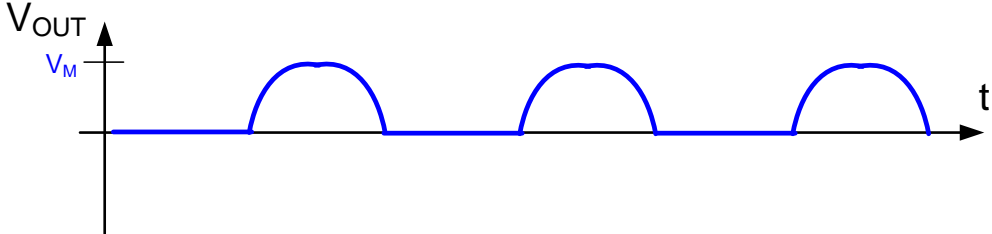
Performance Limitations of Diode Rectifier Circuit



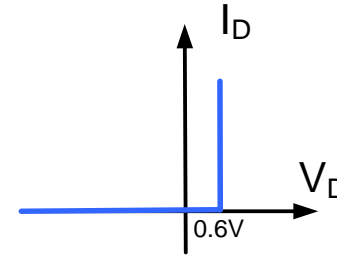
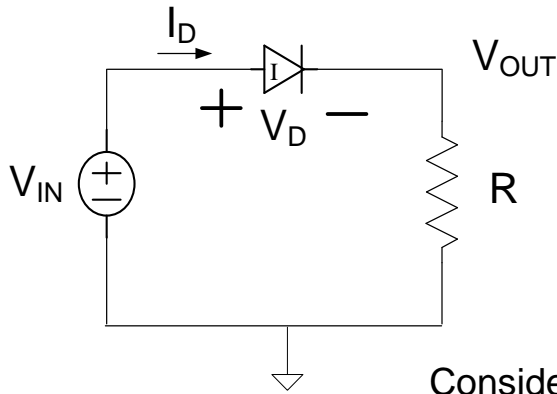
Consider $V_{IN} = V_M \sin \omega t$ for $V_M = 50V$, $V_M = 1V$ and $V_M = 0.5V$



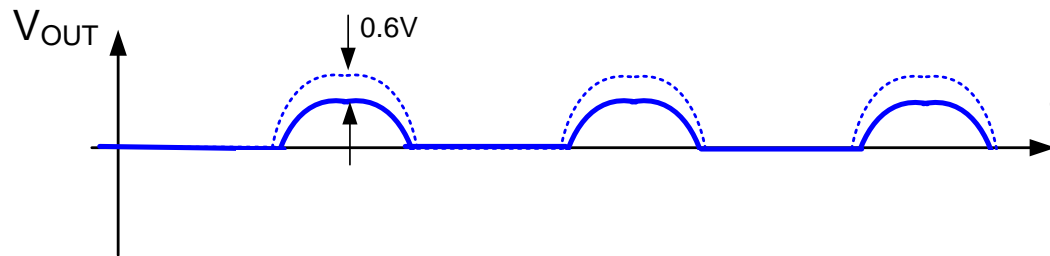
Desired output:



Performance Limitations of Diode Rectifier Circuit

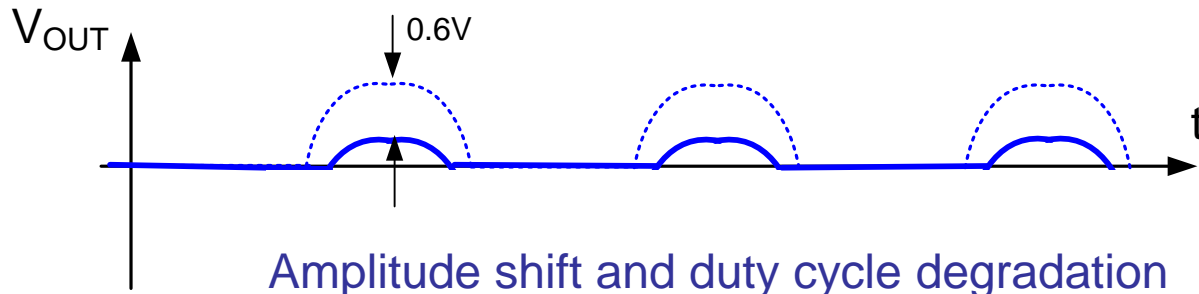


Consider $V_{IN} = V_M \sin \omega t$ for $V_M = 50V$, $V_M = 1V$ and $V_M = 0.5V$



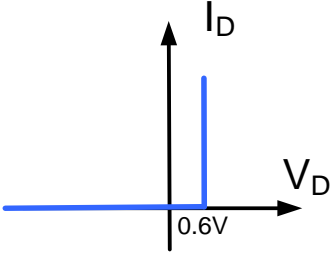
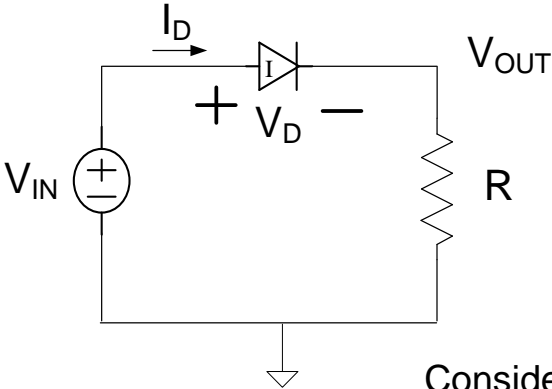
If $V_M = 50V$, the 0.6V drop causes very little degradation in performance

If $V_M = 1V$, the 0.6V drop causes dramatic degradation in performance

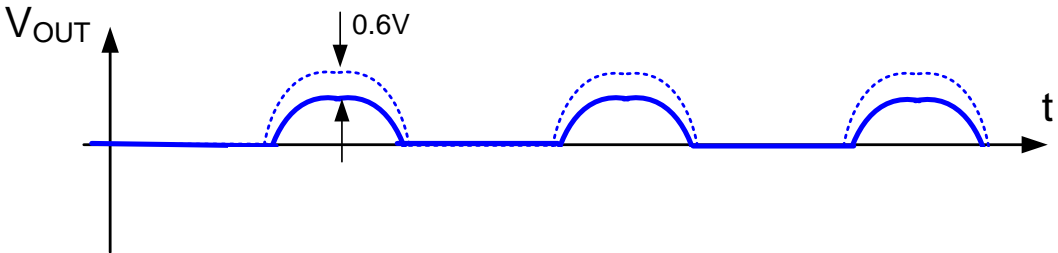


Amplitude shift and duty cycle degradation

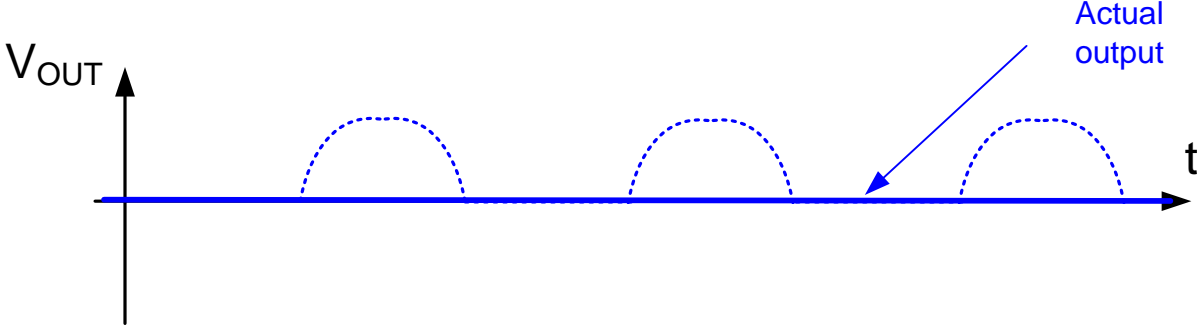
Performance Limitations of Diode Rectifier Circuit



Consider $V_{IN} = V_M \sin \omega t$ for $V_M = 50V$, $V_M = 1V$ and $V_M = 0.5V$

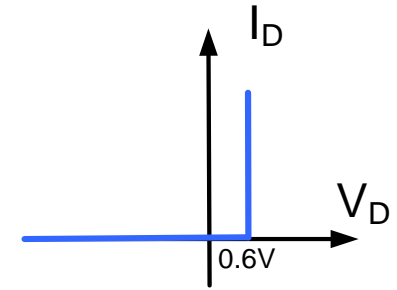
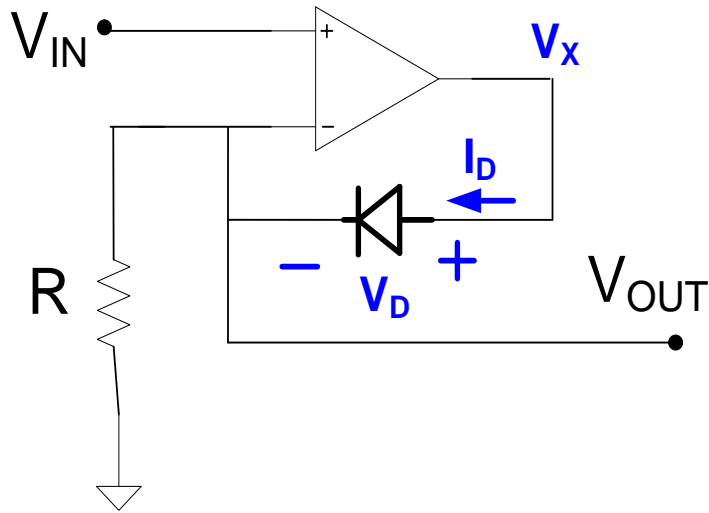


If $V_M = 0.5V$, the 0.6V drop provides no output !



Precision Rectifier Circuit

(with nonideal diode)



$$I_D = 0 \quad V_D < 0.6V$$

$$V_D = 0.6V \quad I_D > 0$$

Case 1 D_1 Conducting, Op Amp operating linearly

$$V_{OUT} = V_{IN}$$

Valid for $I_D > 0$ and

$$V_{SATL} < V_X < V_{SATH}$$

$$I_D = V_{IN} / R$$

$$V_X = V_{OUT} + 0.6V$$

$I_D > 0$ when $V_{IN} > 0$

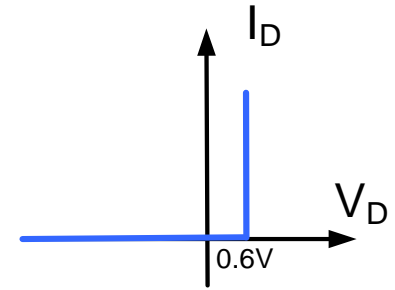
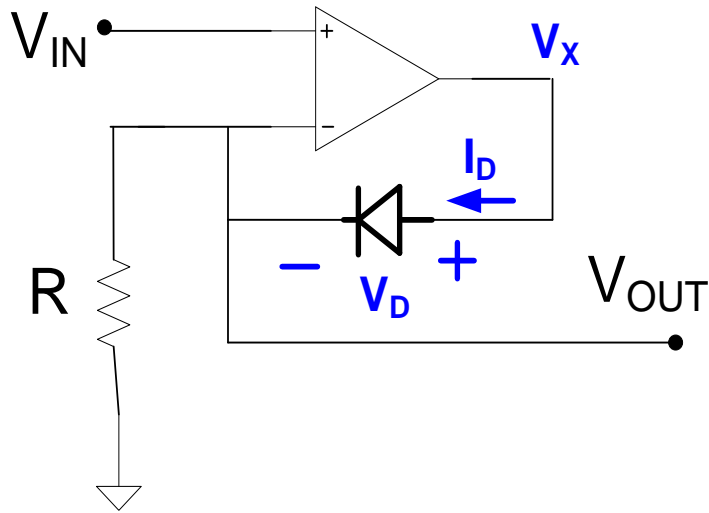
and

$$V_{SATL} - 0.6 < V_{IN} < V_{SATH} - 0.6$$

$$0 < V_{IN} < V_{SATH} - 0.6$$

Precision Rectifier Circuit

(with nonideal diode)

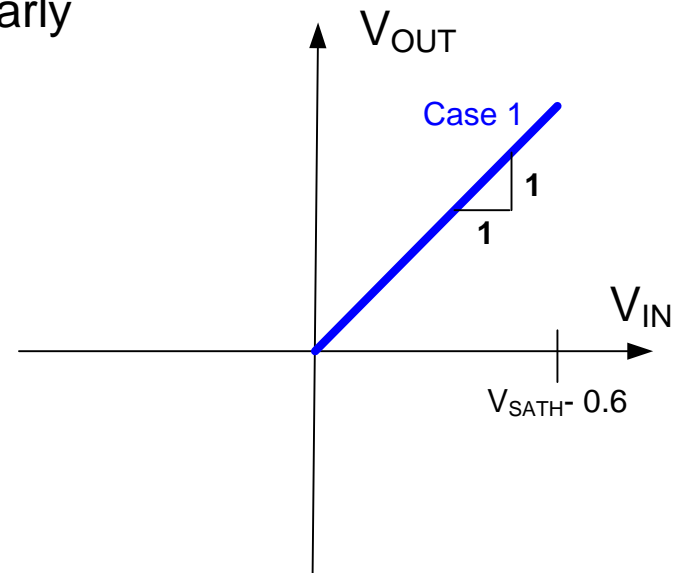


$$I_D = 0 \quad V_D < 0.6V$$
$$V_D = 0.6V \quad I_D > 0$$

Case 1 D_1 Conducting, Op Amp operating linearly

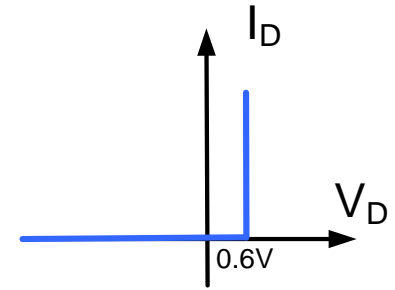
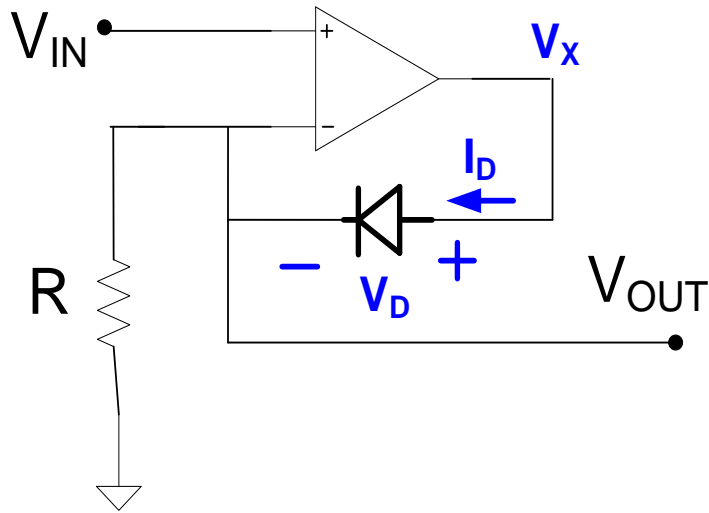
$$V_{OUT} = V_{IN}$$

$$0 < V_{IN} < V_{SATH} - 0.6$$



Precision Rectifier Circuit

(with nonideal diode)



$$I_D = 0 \quad V_D < 0.6V$$

$$V_D = 0.6V \quad I_D > 0$$

Case 2 D_1 Not Conducting, Op Amp saturated low

$$V_{OUT} = 0 \quad (\text{since no current flowing through } R)$$

Valid for $V_D < 0.6V$ and $V^+ < V^-$

$$V_X = V_{SATL}$$

$$V_D = V_X - 0$$

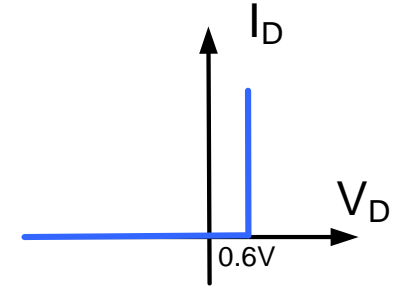
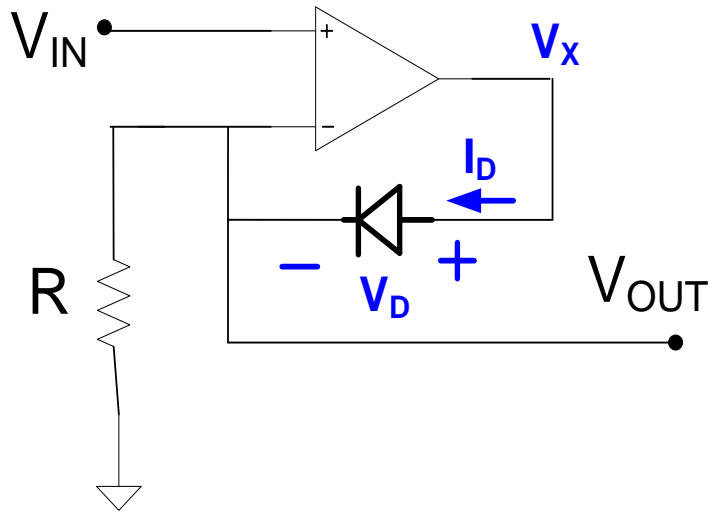
$$V_{IN} < V_{OUT}$$

$V_{SATL} < 0.6V$ and

$$V_{IN} < 0$$

Precision Rectifier Circuit

(with nonideal diode)



$$I_D = 0 \quad V_D < 0.6V$$

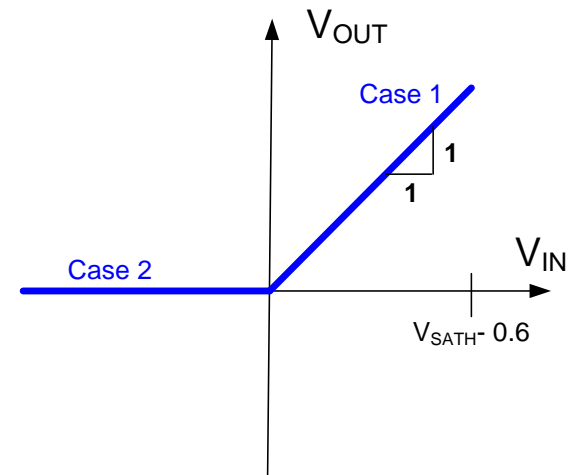
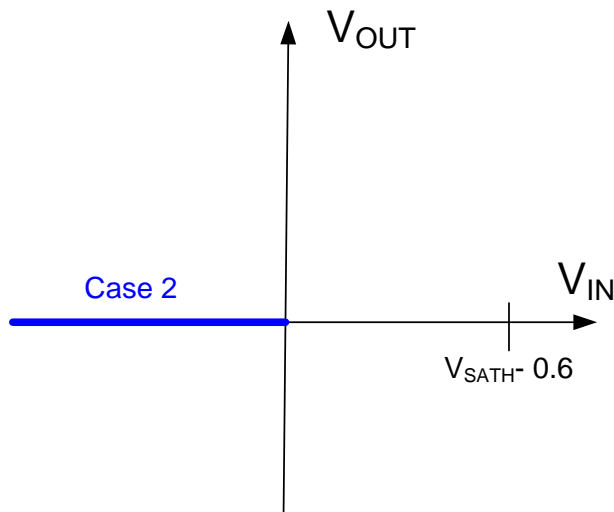
$$V_D = 0.6V \quad I_D > 0$$

Case 2 D_1 Not Conducting, Op Amp saturated low

$$V_{OUT} = 0$$

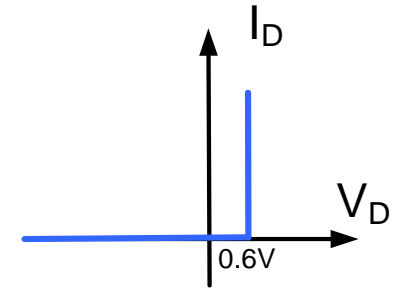
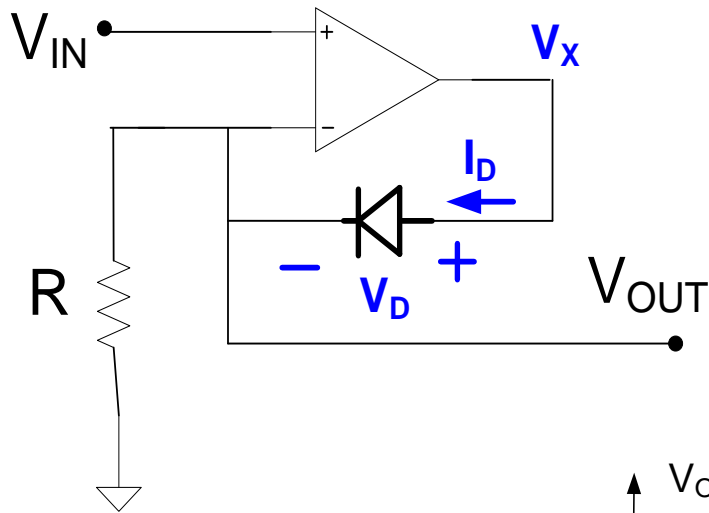
valid for

$$V_{IN} < 0$$

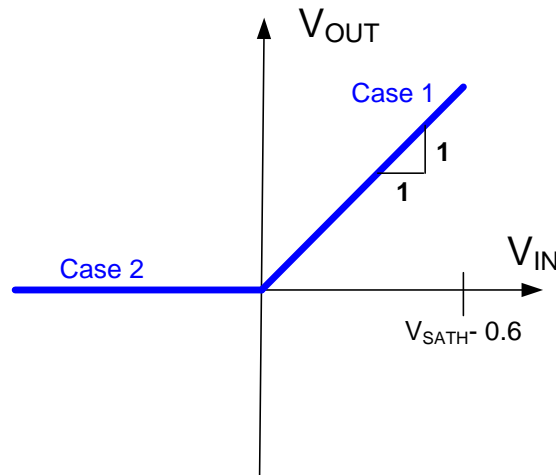


Precision Rectifier Circuit

(with nonideal diode)



$$I_D = 0 \quad V_D < 0.6V$$
$$V_D = 0.6V \quad I_D > 0$$

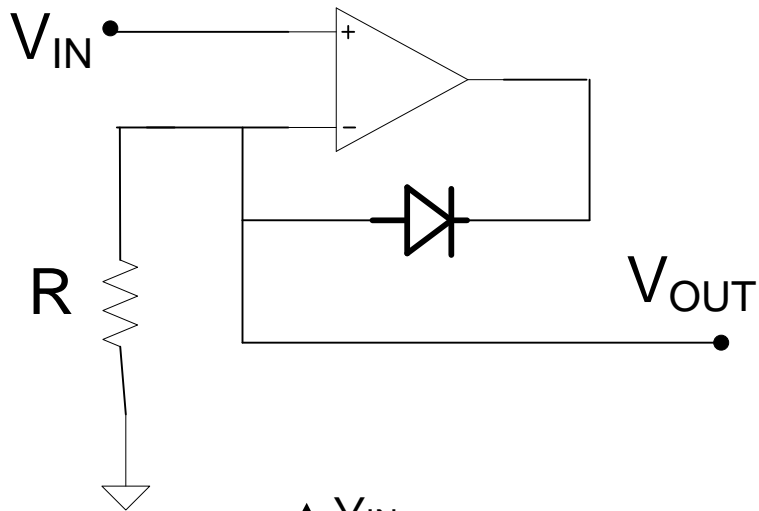


This is the transfer characteristics of an ideal rectifier!

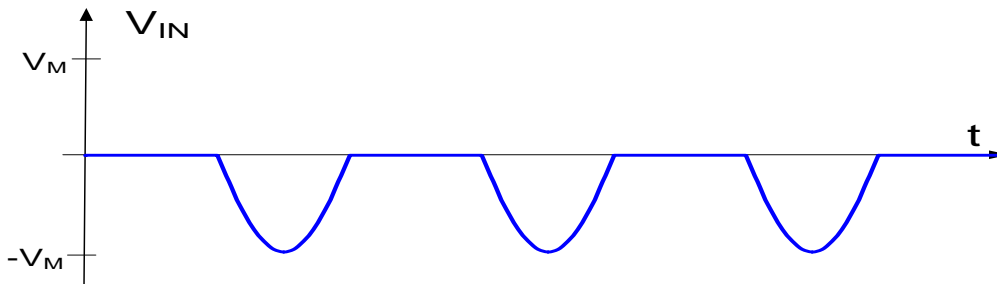
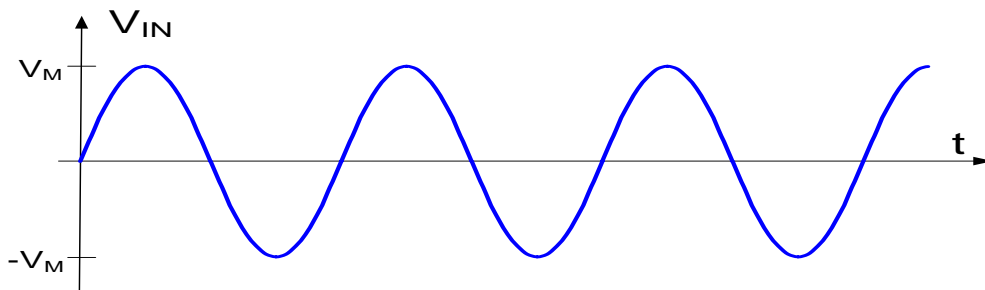
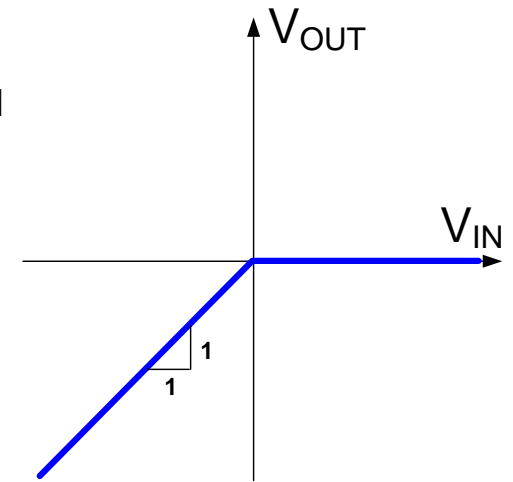
Can be used to rectify very small signals !

Need a buffer on V_{OUT} if any current is to be provided to a load !

Consider this circuit

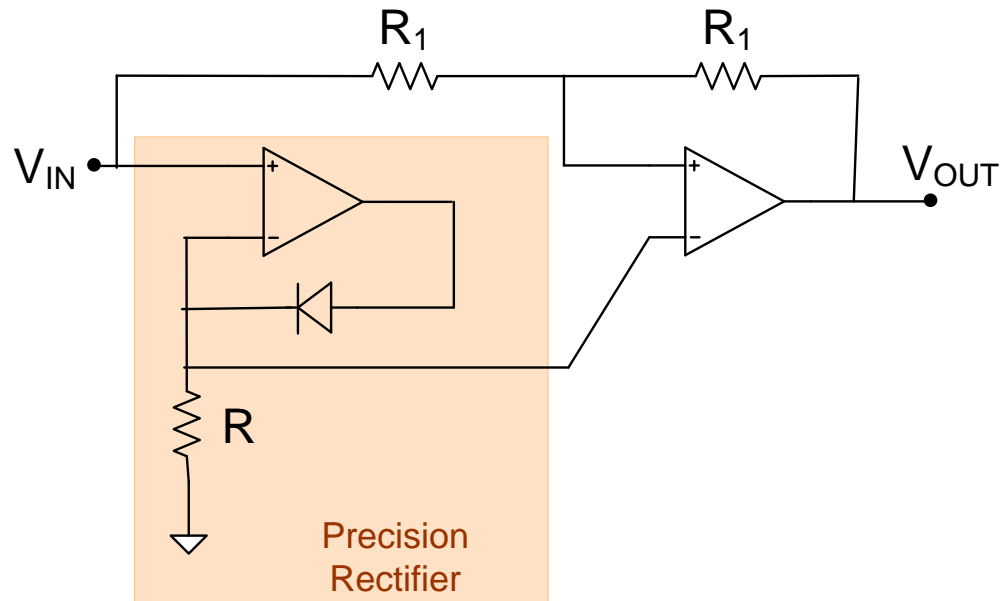
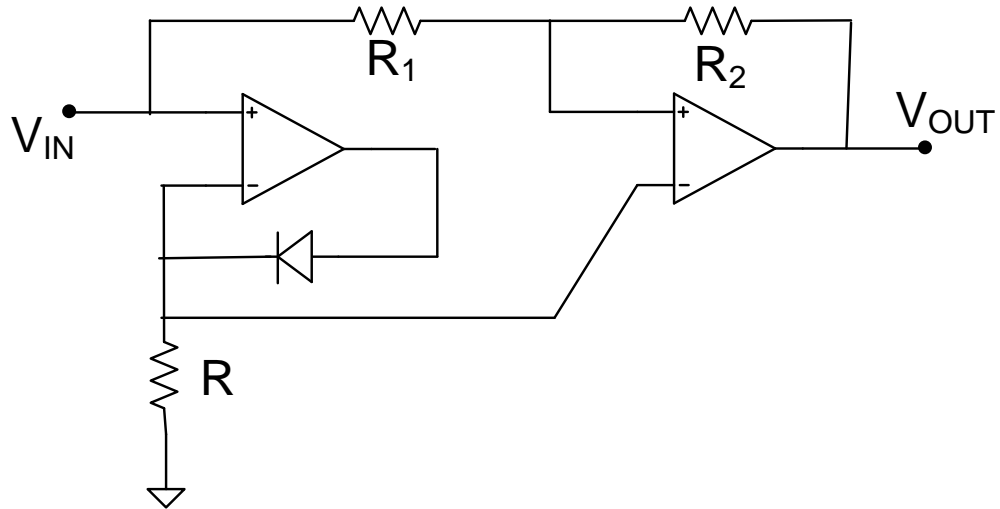


Following an almost identical analysis, can show

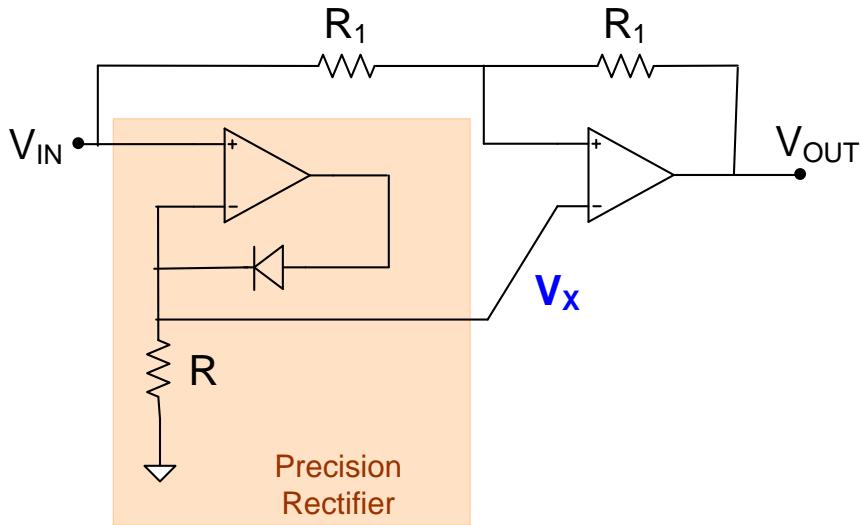


This serves as a precision negative rectifier (not inverting rectifier)

Consider this circuit



Consider this circuit

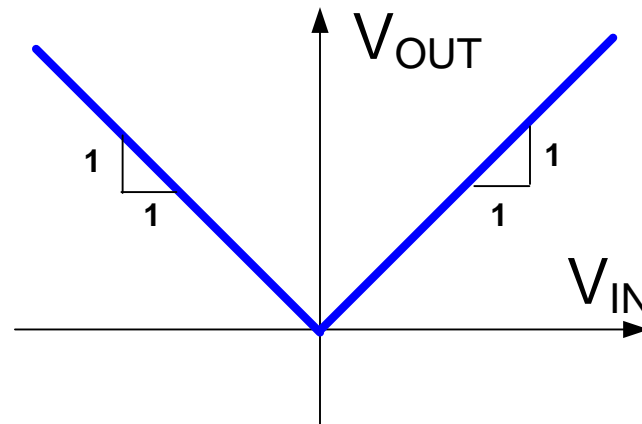


If $V_{IN} > 0$

$V_X = V_{IN}$ so $V_{OUT} = V_{IN}$

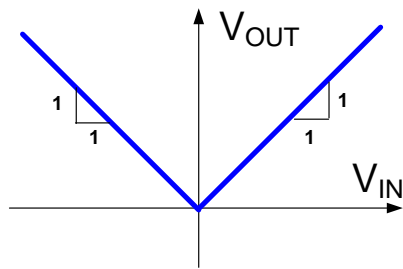
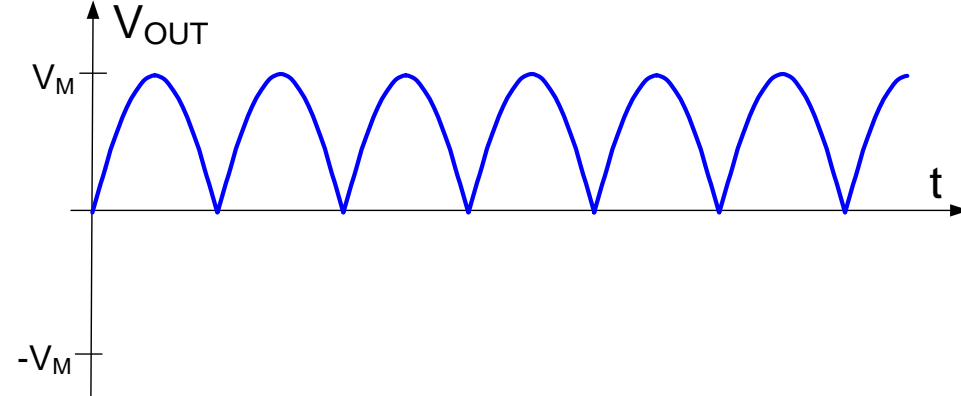
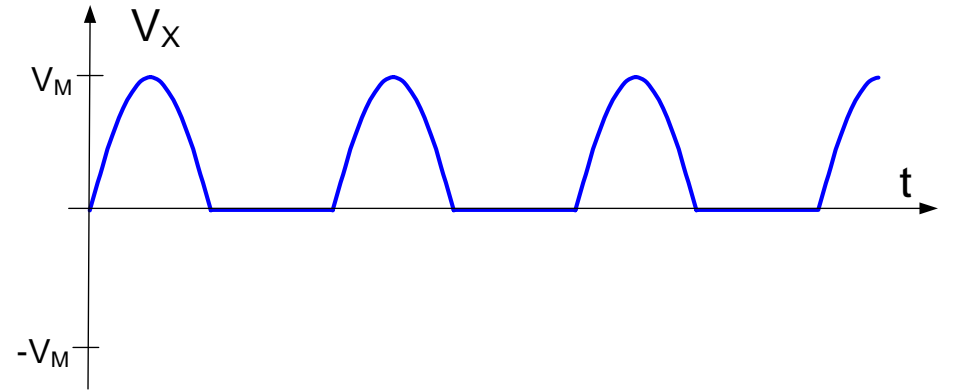
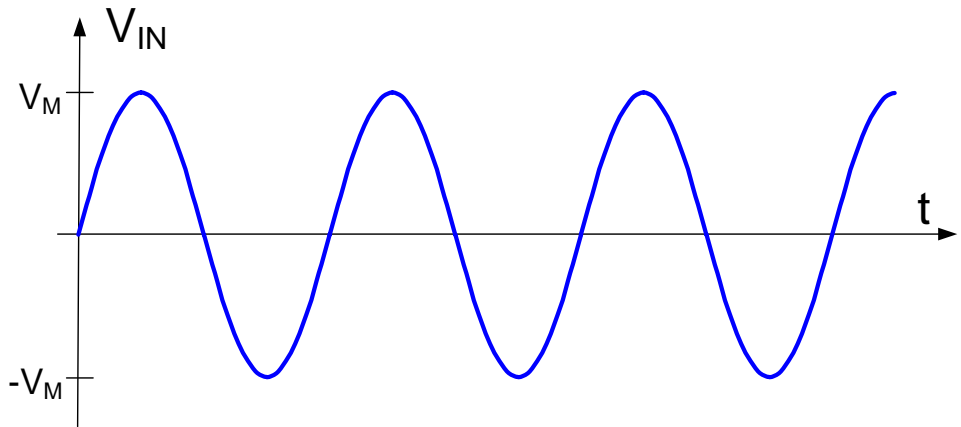
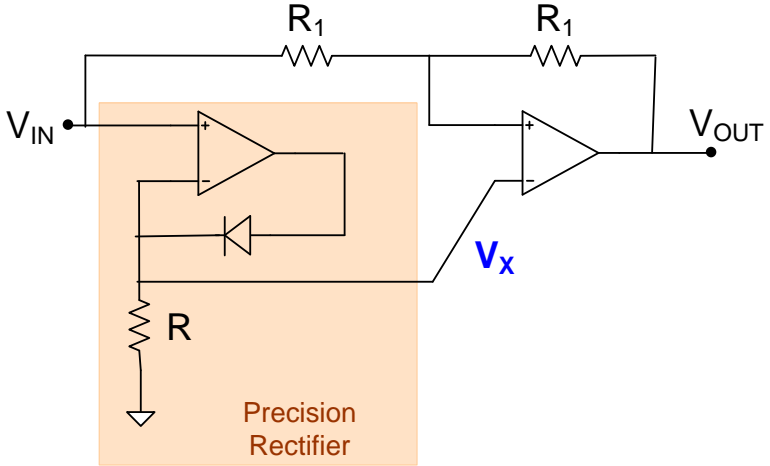
If $V_{IN} < 0$

$V_X = 0$ so $V_{OUT} = -V_{IN}$



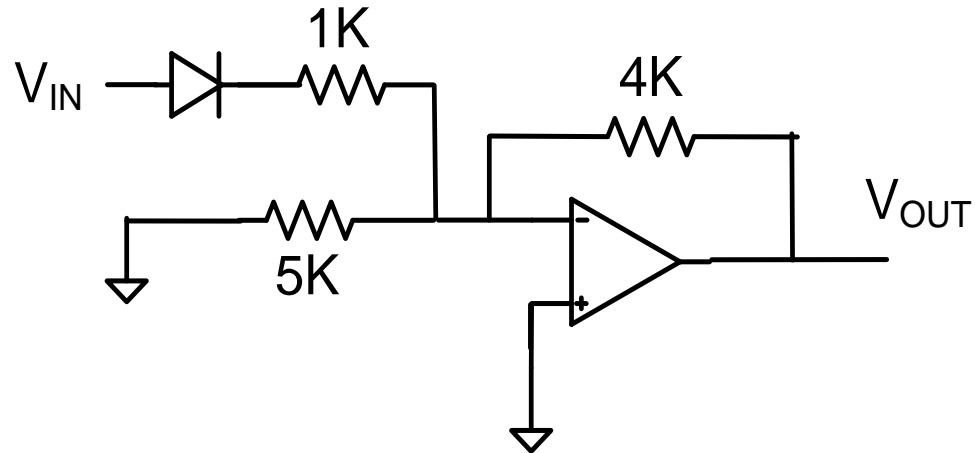
This is a precision full-wave rectifier
(rectifies positive signals, inverts and rectifies negative signals)

Precision Full-Wave Rectifier



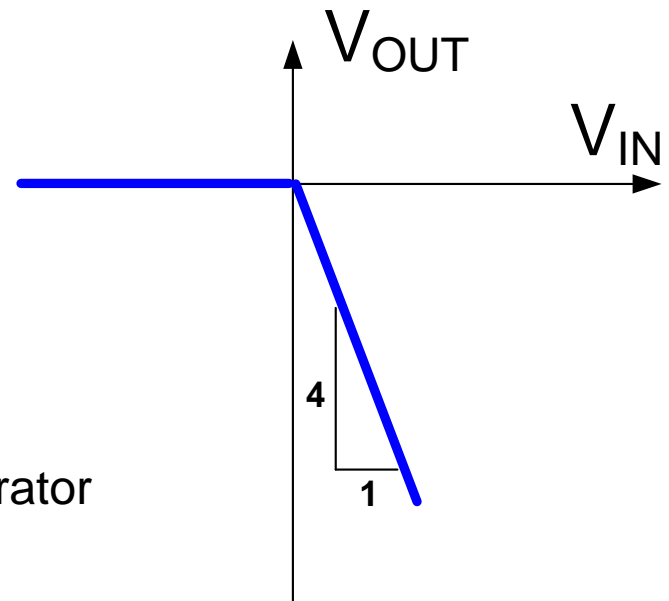
Consider this circuit

(assume diode is ideal)



If diode is OFF, $V_{OUT}=0$

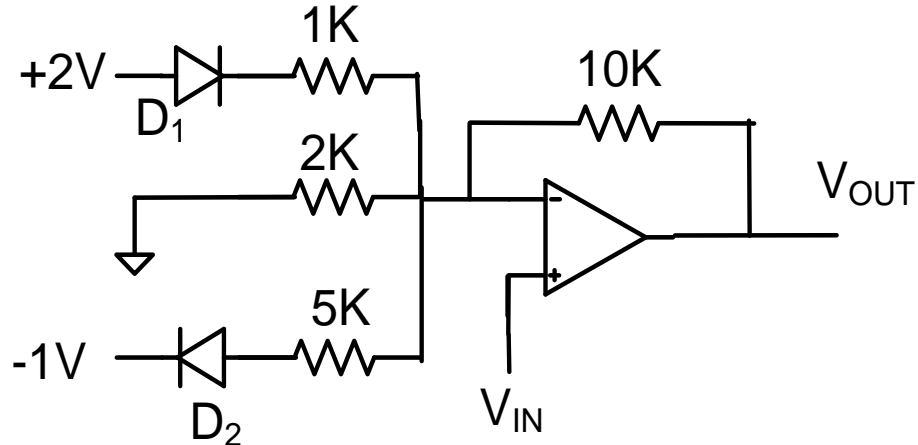
If diode is ON, $V_{OUT} = -10V_{IN}$



- Serves as a two-segment function generator
- But no control of the first slope

Consider this circuit

(assume diodes are ideal)



If $V_{IN} < -1V$, D_1 ON, D_2 OFF

$$V_{OUT} = V_{IN} \left(1 + \frac{10K}{1K//2K} \right) + 2 \left(-\frac{10K}{1K} \right)$$

$$V_{OUT} = V_{IN} \cdot 16 - 20$$

If $2V > V_{IN} > -1V$, D_1 ON, D_2 ON

$$V_{OUT} = V_{IN} \left(1 + \frac{10K}{1K//2K//5K} \right) + 2 \left(-\frac{10K}{1K} \right) - 1V \left(-\frac{10K}{5K} \right)$$

$$V_{OUT} = V_{IN} \cdot 18 - 18$$

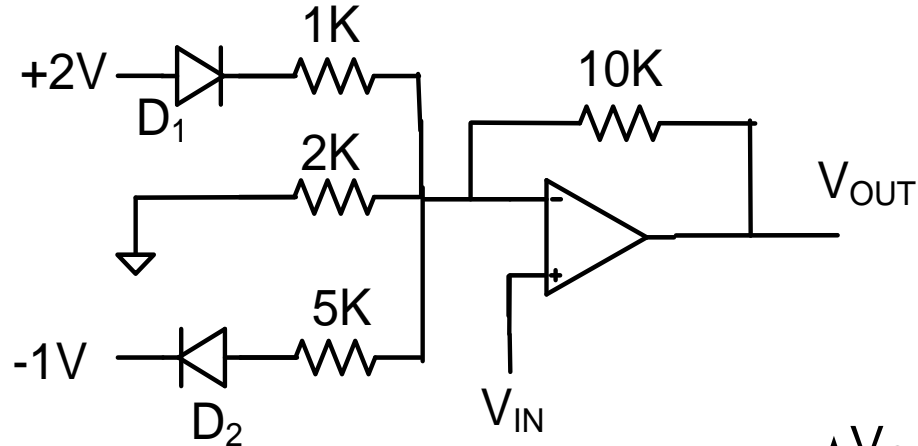
If $V_{IN} > 2V$, D_1 OFF, D_2 ON

$$V_{OUT} = V_{IN} \left(1 + \frac{10K}{2K//5K} \right) + -1V \left(-\frac{10K}{5K} \right)$$

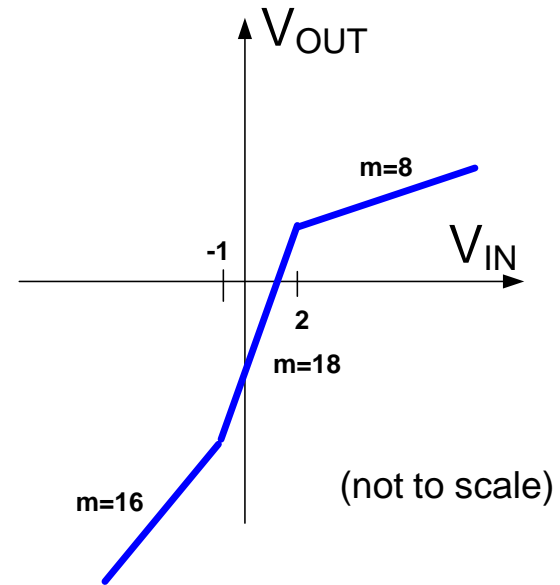
$$V_{OUT} = V_{IN} \cdot 8 + 2$$

Consider this circuit

(assume diodes are ideal)



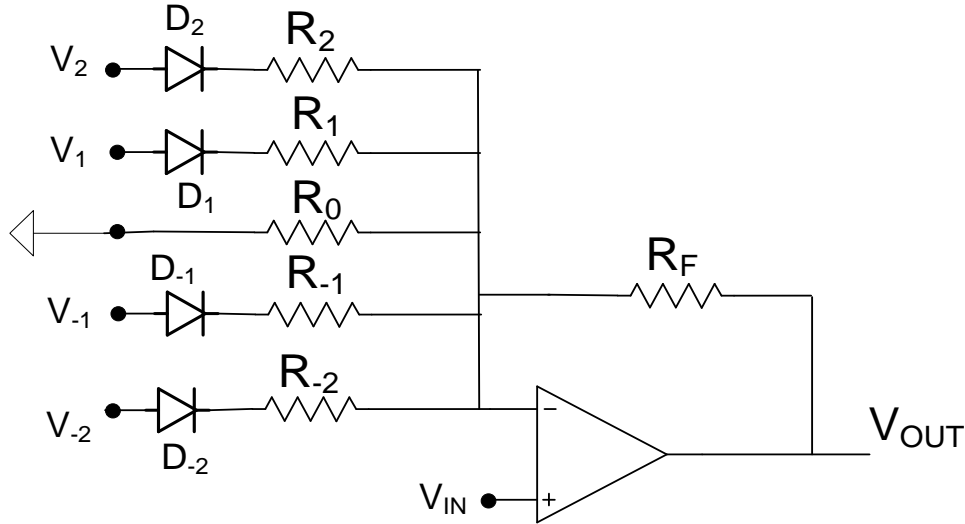
$$V_{OUT} = \begin{cases} 16V_{IN} - 20 & V_{IN} < -1 \\ 18V_{IN} - 18 & -1 < V_{IN} < 2 \\ 8V_{IN} + 2 & V_{IN} > 2 \end{cases}$$



This is a nonlinear function generator

Nonlinear Function Generator

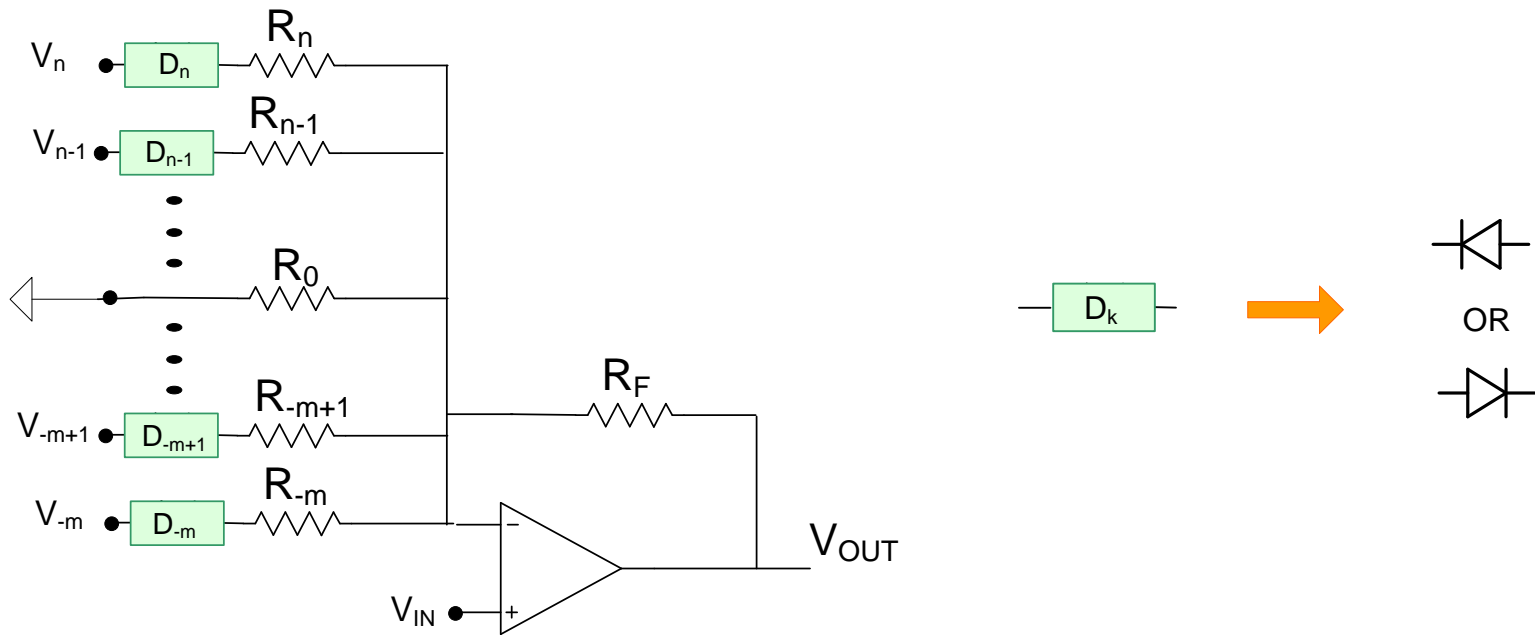
(assume diodes are ideal)



Assume $V_2 > V_1 > V_{-1} > V_{-2}$

- Provides a 5-segment nonlinear function generator
- Analysis straightforward but tedious
- Diode function generators like this can be used to convert a triangle wave to a very good sine wave
- Performance actually usually better with actual diodes since transition between regions is smoother

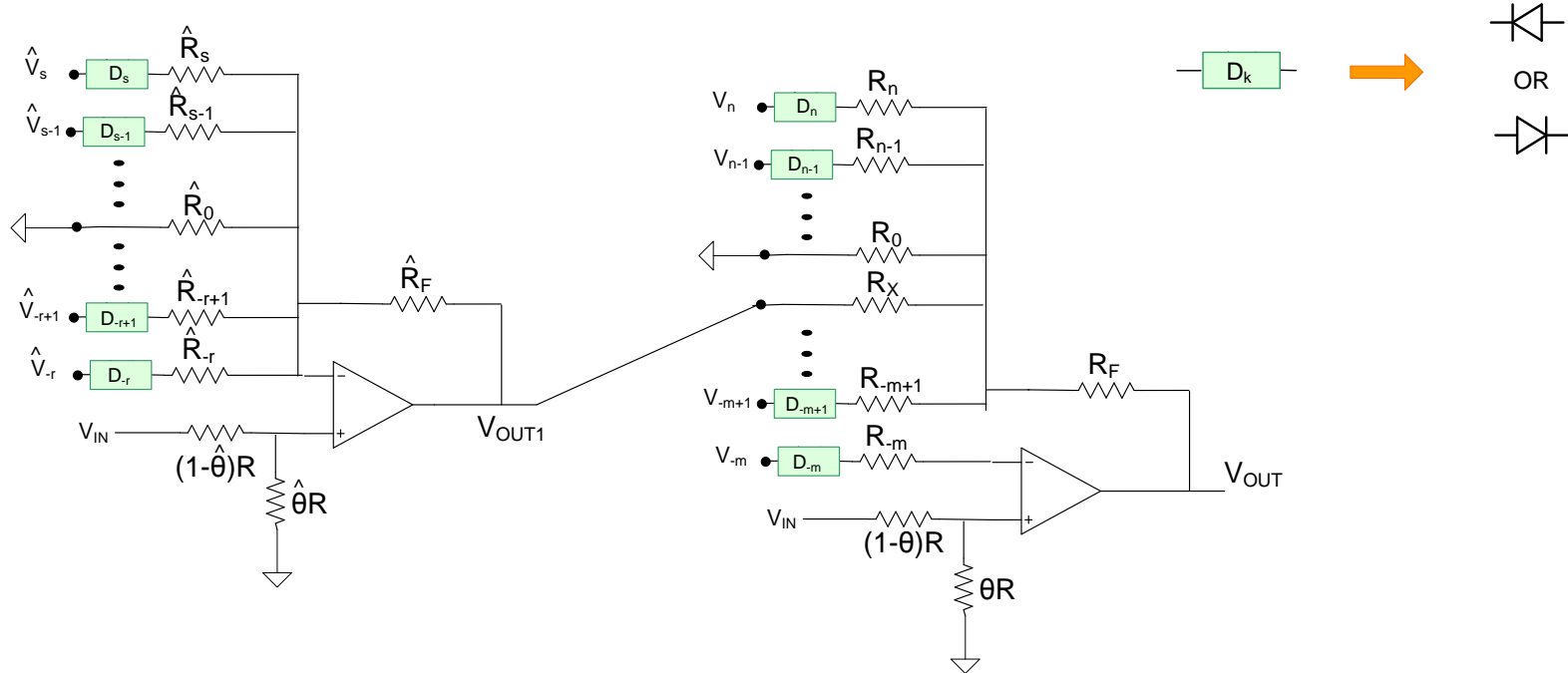
Generalized Nonlinear Function Generator



Assume $V_n > V_{n-1} > \dots > V_1 > 0 > V_{-1} > \dots > V_{-m}$

- Provides $m+n+1$ segment nonlinear function
- Slopes are always positive and greater than 1
- Can generate arbitrary nonlinear transfer characteristic
- Actually works better with nonideal diodes
- Can be extended to provide slopes less than 1
- Can be further extended to provide slopes of arbitrary sign and arbitrary magnitude

Generalized Nonlinear Function Generator



- Provides $m+n+r+s+2$ segment nonlinear function
- Slopes can be positive or negative of any magnitude
- Analysis and design tedious but straight forward

End of Lecture 28